There are six problems each worth 10 points.

1. Suppose $r \geq 2$ is even. Show that no r-regular graph contains a bridge.

2. Given integers m and k where $2 \leq m \leq k$, show that there exists a graph G where m